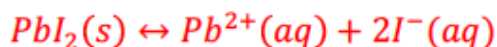


1. A solution is  $1 \times 10^{-4} \text{ M}$  in  $\text{NaI}$ ,  $\text{Na}_2\text{SO}_4$ , and  $\text{Na}_3\text{PO}_4$ . What would the order of precipitation be as a source of  $\text{Pb}^{2+}$  is added gradually to the solution? The relevant  $K_{\text{sp}}$  values are:  $K_{\text{sp}} \text{PbI}_2 = 8.5 \times 10^{-9}$ ;  $K_{\text{sp}} \text{PbSO}_4 = 1.8 \times 10^{-8}$ ;  $K_{\text{sp}} \text{Pb}_3(\text{PO}_4)_2 = 7.9 \times 10^{-43}$ . (Hint: there is no need to use ICE charts here – try to determine where the  $K_{\text{sp}}$  is exceeded)

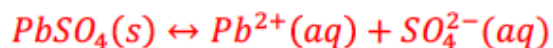
You cannot directly just compare  $K_{\text{sp}}$  values because the cation to anion ratio is not the same!! Setup three different reactions and evaluate each one independently to find the equilibrium  $\text{Pb}^{2+}$  in each case.



$$K_{\text{sp}} = 8.5 \times 10^{-9} = [\text{Pb}^{2+}][\text{I}^{-}]^2 = [\text{Pb}^{2+}](1 \times 10^{-4} \text{ M})^2$$

$$[\text{Pb}^{2+}] = 0.85 \text{ M}$$

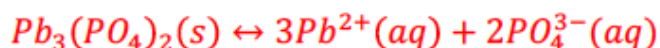
Consider the next solution.



$$K_{\text{sp}} = 1.8 \times 10^{-8} = [\text{Pb}^{2+}][\text{SO}_4^{2-}] = [\text{Pb}^{2+}](1 \times 10^{-4} \text{ M})$$

$$[\text{Pb}^{2+}] = 1.8 \times 10^{-4} \text{ M}$$

And finally, the last solution.



$$K_{\text{sp}} = 7.9 \times 10^{-43} = [\text{Pb}^{2+}]^3[\text{PO}_4^{3-}]^2 = [\text{Pb}^{2+}]^3(1 \times 10^{-4} \text{ M})^2$$

$$[\text{Pb}^{2+}] = 4.29 \times 10^{-12} \text{ M}$$

To determine the order of precipitation, the one that has the lowest equilibrium  $\text{Pb}^{2+}$  concentration is the one that will precipitate first since  $\text{Pb}^{2+}$  is being added gradually. Thus, the order of precipitation is:

#1  $\text{Pb}_3(\text{PO}_4)_2$

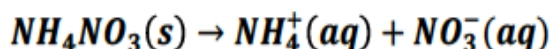
#2  $\text{PbSO}_4$

#3  $\text{PbI}_2$

2. Fill in the blanks in the following table. Both  $\Delta H$  and  $\Delta S$  refer to the system.

$\Delta H$	$\Delta S$	$\Delta G$	Low Temp	High temp
-	+	-	Spontaneous	Spontaneous
-	-	Temp. dependent	Spontaneous	Non-spontaneous
+	+	Temp. dependent	Non-spontaneous	Spontaneous
+	-	+	Non-spontaneous	Non-spontaneous

3. Calculate  $\Delta H^\circ$ ,  $\Delta S^\circ$ , and  $\Delta G^\circ$  for the following reaction to determine if it is spontaneous at  $25^\circ\text{C}$ .



Compound	$\Delta H_f^\circ$ (kJ/mol)	$\Delta S^\circ$ (J/K*mol)
$\text{NH}_4\text{NO}_3$ (s)	-365.56	151.08
$\text{NH}_4^+$ (aq)	-132.51	113.4
$\text{NO}_3^-$ (aq)	-205.0	146.4

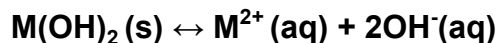
$$\begin{aligned}
 \Delta H^\circ &= \Delta H_f^\circ \text{ products} - \Delta H_f^\circ \text{ reactants} \\
 &= \left[ \left( 1 \text{ mol } \text{NH}_4^+ * -132.51 \frac{\text{kJ}}{\text{mol}} \right) + \left( 1 \text{ mol } \text{NO}_3^- * -205.0 \frac{\text{kJ}}{\text{mol}} \right) \right] \\
 &\quad - \left[ 1 \text{ mol } \text{NH}_4\text{NO}_3 * -365.56 \frac{\text{kJ}}{\text{mol}} \right] = 28.05 \text{ kJ}
 \end{aligned}$$

$$\begin{aligned}\Delta S^\circ &= \Delta S^\circ_{\text{products}} - \Delta S^\circ_{\text{reactants}} \\ &= \left[ \left( 1 \text{ mol } NH_4^+ * 113.4 \frac{J}{\text{mol} * K} \right) + \left( 1 \text{ mol } NO_3^- * 146.4 \frac{J}{\text{mol} * K} \right) \right] \\ &\quad - \left[ 1 \text{ mol } NH_4NO_3 * 151.08 \frac{J}{\text{mol} * K} \right] = 108.72 \frac{J}{K}\end{aligned}$$

$$\Delta G^\circ = \Delta H^\circ - T\Delta S^\circ = 28.05 \text{ kJ} - (298.15 \text{ K}) \left( 0.10872 \frac{\text{kJ}}{K} \right) = -4.36 \text{ kJ}$$

Since  $\Delta G^\circ$  is negative, the reaction is spontaneous.

4. An unknown metal M forms an ionic hydroxide with the formula  $M(OH)_2$  that exhibits the equilibrium...



...in a saturated aqueous solution. If the solution pH is 10, what is the solubility product constant  $K_{sp}$  of the compound?

$$\text{The } K_{sp} = [M^{2+}][OH^-]^2$$

If pH is 10, it means pOH is 4 and  $[OH^-]$  is  $10^{-4}$ . According to stoichiometry, the  $[M^{2+}]$  must be  $5 \cdot 10^{-5}$ . Plugging this into the equation yields  $K_{sp} = [5 \cdot 10^{-5}][10^{-4}]^2 = 5 \times 10^{-13}$

5. If the solubility product constant  $K_{sp}$  for  $NaC_9H_7O_4$  is estimated to be 34.9, what is the approximate acetylsalicylate ion concentration in a saturated  $NaC_9H_7O_4$  solution used for the reaction?

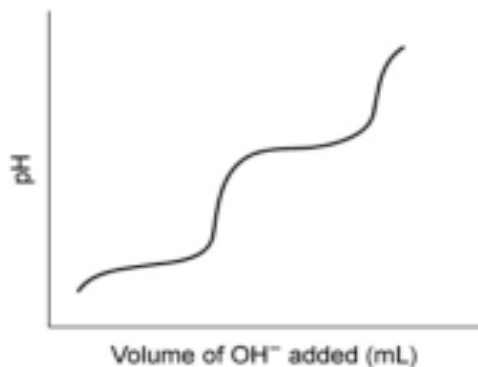
5.91 M

$$K_{sp} = [Na^+][C_9H_7O_4^-]$$

Since the sodium and acetylsalicylate ions form the compound of interest in a 1:1 ratio,  $K_{sp} = x^2$      $x = 5.91 \text{ M}$

## MCAT Style Questions

6. The figure below shows the titration curve for an acid titrated with aqueous sodium hydroxide. When titrated in solution, which of the following salts would be most likely to produce a similar titration curve?



- a.  $(\text{NH}_4)_3\text{PO}_4$
- b.  $\text{KH}_2\text{PO}_4$
- c.  $\text{Na}_2\text{HPO}_4$
- d.  $\text{K}_3\text{PO}_4$

7. Suppose that citric acid ( $\text{H}_3\text{C}_6\text{H}_5\text{O}_7$ ) is titrated with 0.1 M NaOH to form a citrate buffer solution with a pH of 4.5. What is the pH at the first equivalence point? (Note:  $\text{pK}_{\text{a}1} = 3.13$ ,  $\text{pK}_{\text{a}2} = 4.76$ ,  $\text{pK}_{\text{a}3} = 6.40$ )

- a. Less than 3.13
- b. Between 3.13 and 4.76
- c. Equal to 3.13
- d. Greater than 4.76

8. Which of the following compound pairs, dissolved into solution at equal concentrations, will function as a buffer?

- a.  $\text{CH}_3\text{COOH}$  (aq) and  $\text{CH}_3\text{COONa}$  (aq)
- b.  $\text{HNO}_3$  (aq) and  $\text{NaNO}_3$  (aq)
- c.  $\text{NaBr}$  (aq) and  $\text{NaCN}$  (aq)
- d.  $\text{NaOH}$  (aq) and  $\text{NaCl}$  (aq)

9. Consider a solution of magnesium hydroxide,  $K_{\text{sp}} = 8.9 \times 10^{-12}$ . solid magnesium hydroxide begins to precipitate when which of the following expressions is true?

- a.  $[\text{OH}^-] < 1 \times 10^{-7}$
- b.  $[\text{Mg}^{2+}] = 8.9 \times 10^{-12}$
- c.  $[\text{OH}^-] = [\text{Mg}^{2+}]$
- d.  $[\text{Mg}^{2+}][\text{OH}^-]^2 > 8.9 \times 10^{-12}$

10. Suppose that a research technician wants to separate an aqueous mixture of  $\text{CuF}_2$  and  $\text{BaF}_2$  ( $K_{\text{sp}} = 3.0 \times 10^{-6}$ ) by precipitating  $\text{CuF}_2$  from the solution. What should be added to the solution to perform the separation?

- a.  $\text{Cu}(\text{NO}_3)_2$

b. NaF

c. Ba(NO<sub>3</sub>)<sub>2</sub>

d. H<sub>2</sub>O