

Late 1800s/early 1900s - Interaction b/w matter and light was under investigation

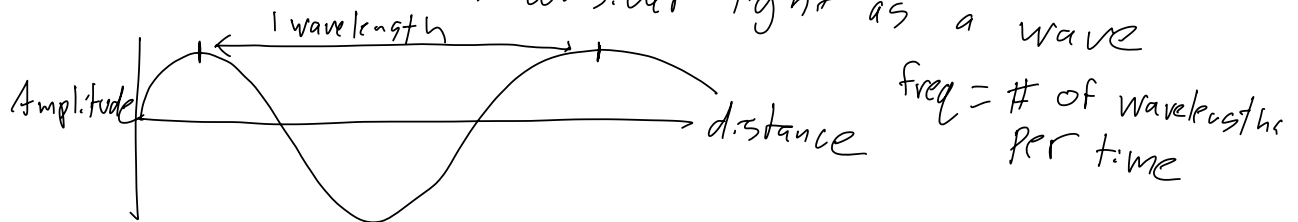
light = radiation

wavelength ( $\lambda$ ) distance

frequency ( $\nu$ )  $1/\text{time}$

velocity ( $c$ ) dist/time

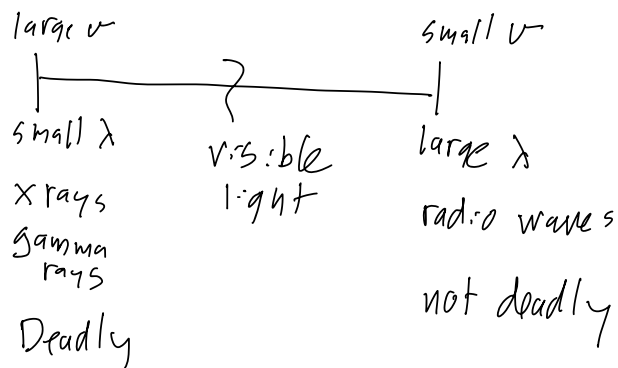
For the moment lets consider light as a wave



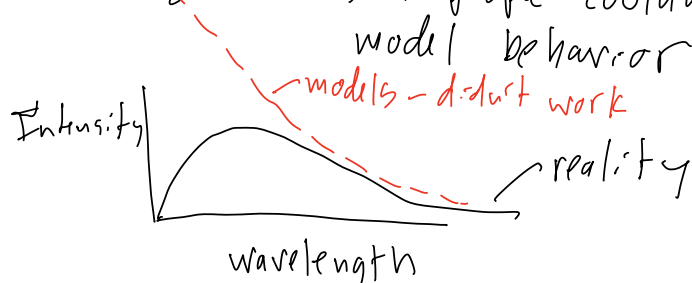
velocity of light is constant

$$c = 3 \times 10^8 \text{ m/sec}$$

$$c = \lambda \nu$$



Hot things glow - but people couldn't successfully model behavior



Max Planck - new model - that worked

- heated molecules/atoms vibrate and give off light
- only some vibrational frequencies possible so only some freq (or wavelengths) of light could be given off
- Frequency (or wavelength) related to energy
- so only certain energies are possible

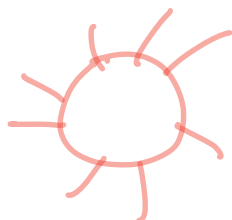
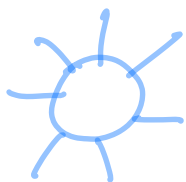
Energy of radiation is quantized

$$E = nh\nu$$

integer = # of "pieces" of radiation  
frequency in  $\text{sec}^{-1}$   
Planck's constant =  $6.626 \times 10^{-34} \text{ J} \cdot \text{sec}$   
Energy of radiation

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Einstein + photoelectric effect - shine light on metal make electricity flow



lots of electricity

no electricity

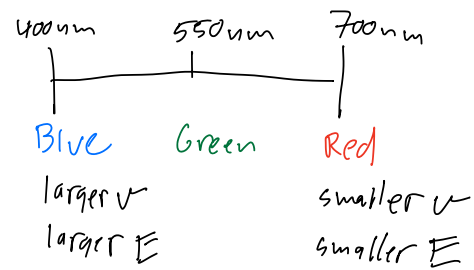
some electricity

no electricity

Einstein - light isn't a wave but is a massless particle  $\rightarrow$  photon

$$E_{\text{photon}} = h\nu \text{ or } \frac{hc}{\lambda} \text{ b/c } c = \lambda\nu$$

"wave particle duality"



If we had blue light

$$\lambda = 450 \text{ nm}$$

$$E_{\text{photon}} = h \nu$$

$$3 \times 10^8 \text{ m/sec} = (450 \times 10^{-9} \text{ m})(\nu)$$

$$\nu = \frac{3 \times 10^8 \text{ m/sec}}{450 \times 10^{-9} \text{ m}} = 6.6 \times 10^{14} \text{ sec}^{-1}$$

$$E = (6.626 \times 10^{-34} \text{ J} \cdot \text{sec})(6.6 \times 10^{14} \text{ sec}^{-1})$$

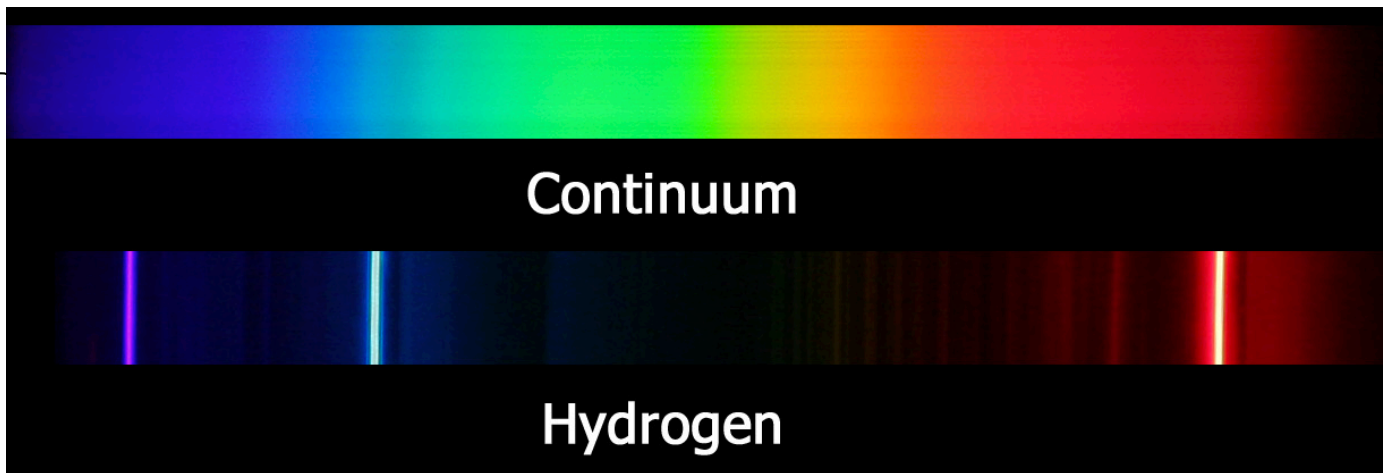
$$E = 4.4 \times 10^{-19} \text{ J}$$

# Atomic Line Spectrum from Hydrogen Discharge Lamp



- tube filled w/  $H_2$
- electrodes @ top + bottom
- high voltage
- $H_2$  split into  $H$  atoms
- atoms glow

white light

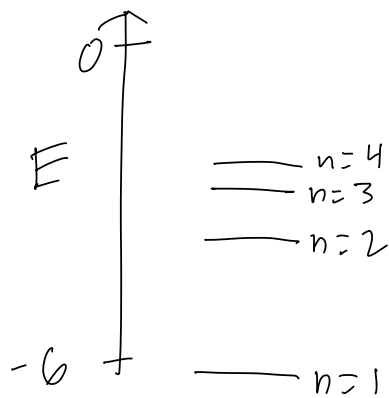


3 lines means light from discharge lamp is made up of 3 different types of photons

Imagine  $e^-$  in  $H$  atom has different energy levels it can live at  
Adding energy causes  $e^-$  to go up a level or more



Being at higher energy isn't sustainable  
 so electron eventually falls back down, giving  
 off energy by emitting a photon of light



$$E_n = -\frac{Rhc}{n^2}$$

Rydberg constant  
 $1.097 \times 10^7 \text{ m}^{-1}$

Energy of  $n^{\text{th}}$  level

$n$  from  $n^{\text{th}}$  level

higher  $\rightarrow$  lower energy given off as photon

lower  $\rightarrow$  higher energy of photon taken in to allow  $e^-$  to move up

## Wave particle duality part 2

under certain circumstances particles can be described in wave-like ways

$$\lambda_{\text{particle}} = \frac{h}{m v}$$

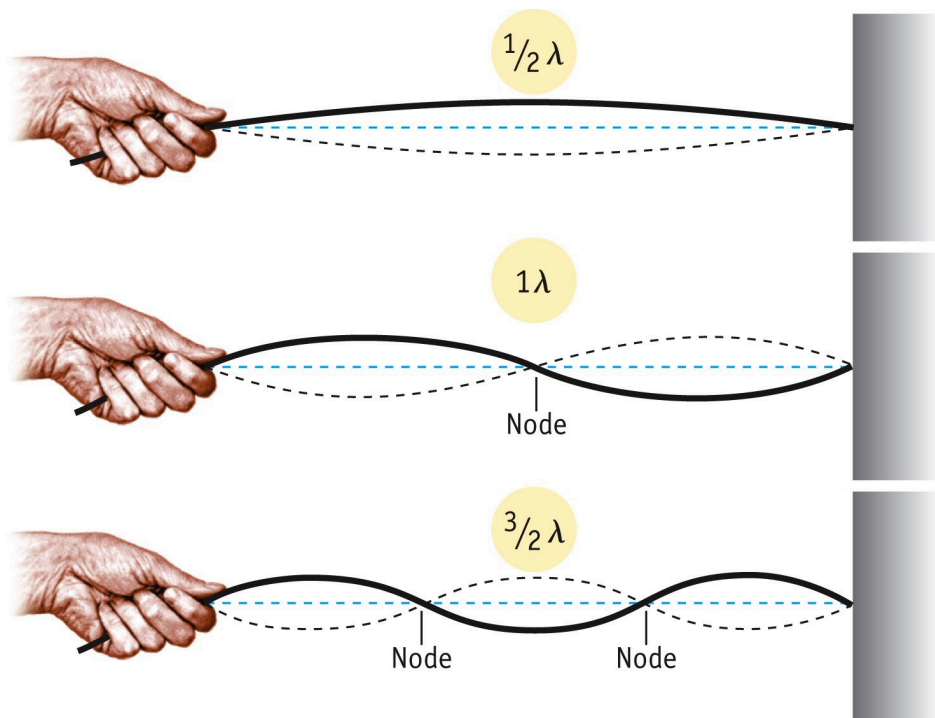
DeBroglie wavelength

$m$  mass of particle  
 $v$  velocity of particle

Quantum mechanics is how we describe electrons  
 - math but no math

Standing wave is concept to describe electrons  $\rightarrow$  only certain  $\lambda$  possible for a standing wave

$\rightarrow$  only certain energies are possible



Wave motion: wave length and nodes  
"Quantization" in a standing wave

Electrons described as 3-D standing wave  
Wavefunction ( $\Psi$ ) is the math equation for the standing wave

$$\Psi = 42x^4 + 13y^{3/2} - 7z^8$$

for each  $(x, y, z)$  point in space  $\Psi$  has amplitude

$\Psi^2$  - tells you probability of electron being at particular place in 3-D space

-electrons only described in terms of probability  
Use quantum numbers as shorthand to describe  
Wave Functions

$n$  = principal quantum # "shell"

$n = 1, 2, 3, 4, \dots$

describes energy

describes extent of spatial probability distribution

$l$  = orbital angular momentum QN "subshell"

$l = 0, 1, 2, \dots, n-1$

describes shape

$l = 0 \rightarrow s$

$l = 1 \rightarrow p$

$l = 2 \rightarrow d$

$l = 3 \rightarrow f$

$m_l$  = magnetic QN

$m_l = -l, \dots, +l$

describes orientation in 3-D space

If  $n=1$   $l$  must  $= 0$  and  $m_l$  must be zero  
 only 1  $\psi$  when  $n=1 \rightarrow n=1, l=0, m_l=0$

If  $n=2$   $l$  could be 0 or 1  
 $\downarrow$   $\downarrow$   
 $m_l=0$   $m_l=-1, 0, 1$

$\frac{n}{2}$	$\frac{l}{0}$	$\frac{m_l}{0}$	
2	0	0	
2	1	-1	4 possible $\psi$ when $n=2$
2	1	0	
2	1	1	

$n=3$   $l=0, 1, 2$   
 $\downarrow$   $\downarrow$   $\searrow$   
 $m_l=0$   $m_l=-1, 0, 1$   $m_l=-2, -1, 0, 1, 2$

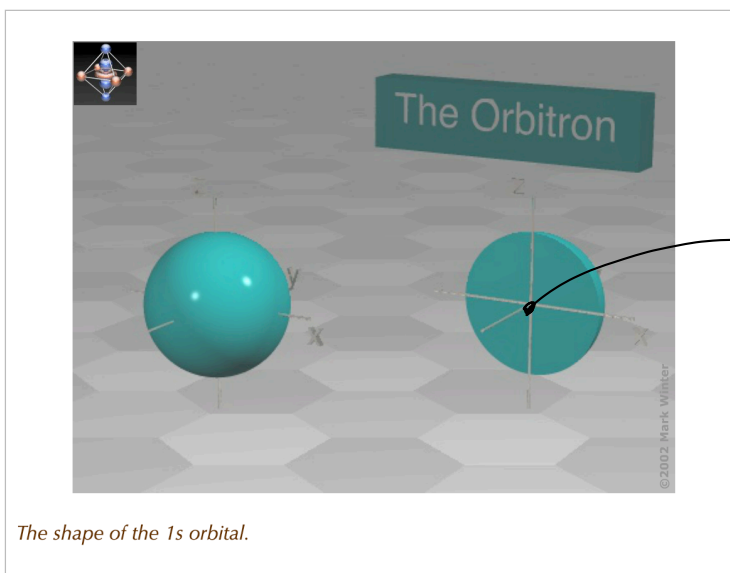
$\frac{n}{3}$	$\frac{l}{0}$	$\frac{m_l}{0}$	
3	0	0	
3	1	-1	9 possible $\psi$ when $n=3$
3	1	0	
3	1	1	
3	2	-2	
3	2	-1	
3	2	0	
3	2	1	
3	2	2	
3	2	2	

orbital = wavefunction

$l=0$   
**1s orbital**

$n=1$   
 $l=0$   
 $m_l=0$

### Atomic orbitals: 1s

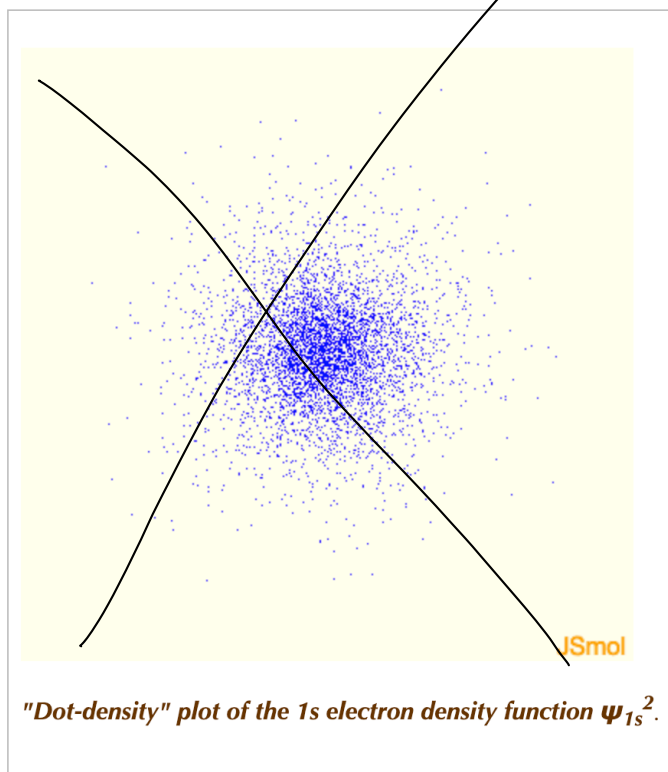


$s \rightarrow$  spherical

nucleus

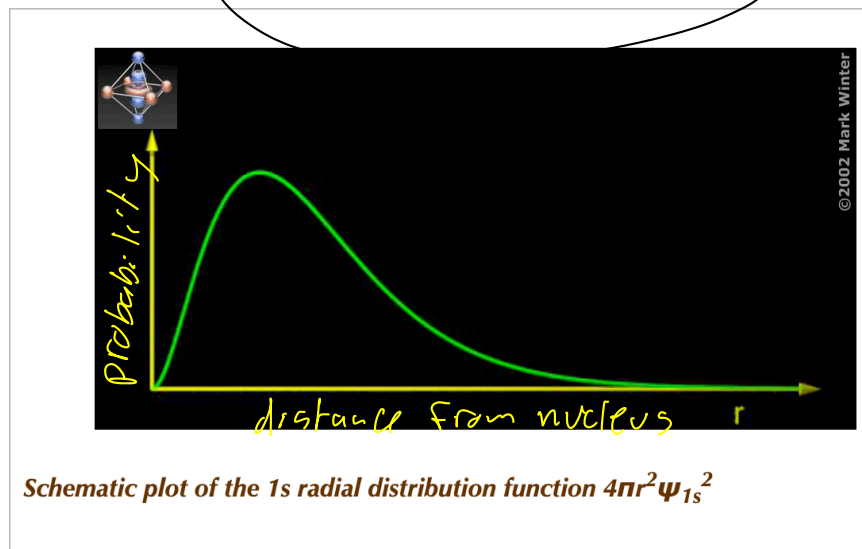
For any atom there is just one 1s orbital. Consider the charge on the left. The surface of

### Atomic orbitals: 1s electron density

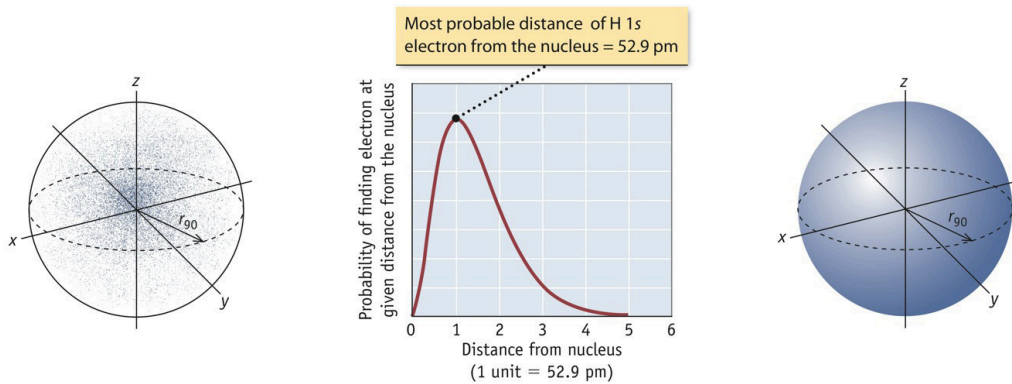


probability of finding  $e^-$  at particular distance from nucleus

### Atomic orbitals: 1s radial distribution function



# s-Orbitals



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- $l = 0, m_l = 0$
- $2l + 1 = 1$
- one s-orbital that extends in a radial manner from the nucleus forming a spherical shape.

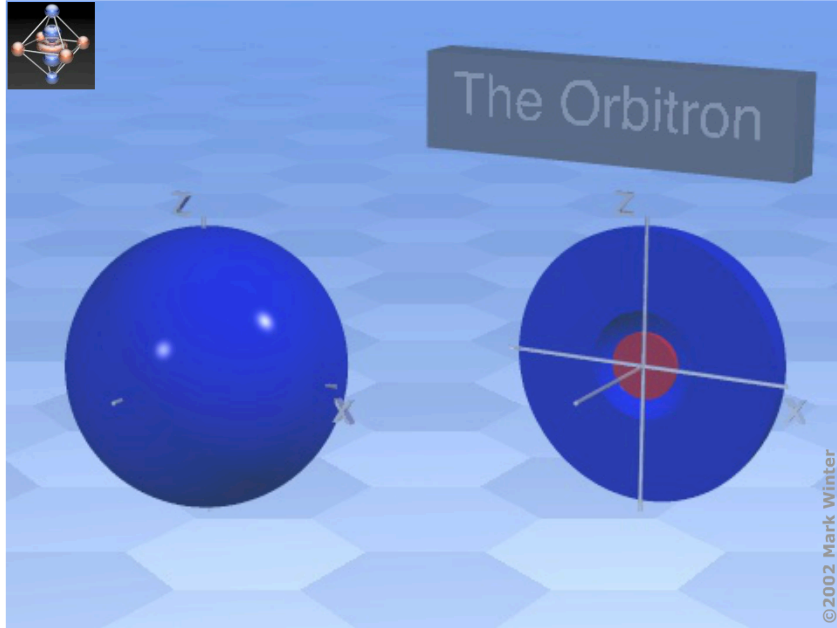
# 2s orbital

$$n=2$$

$$l=0$$

$$m_l=0$$

Atomic orbitals: 2s

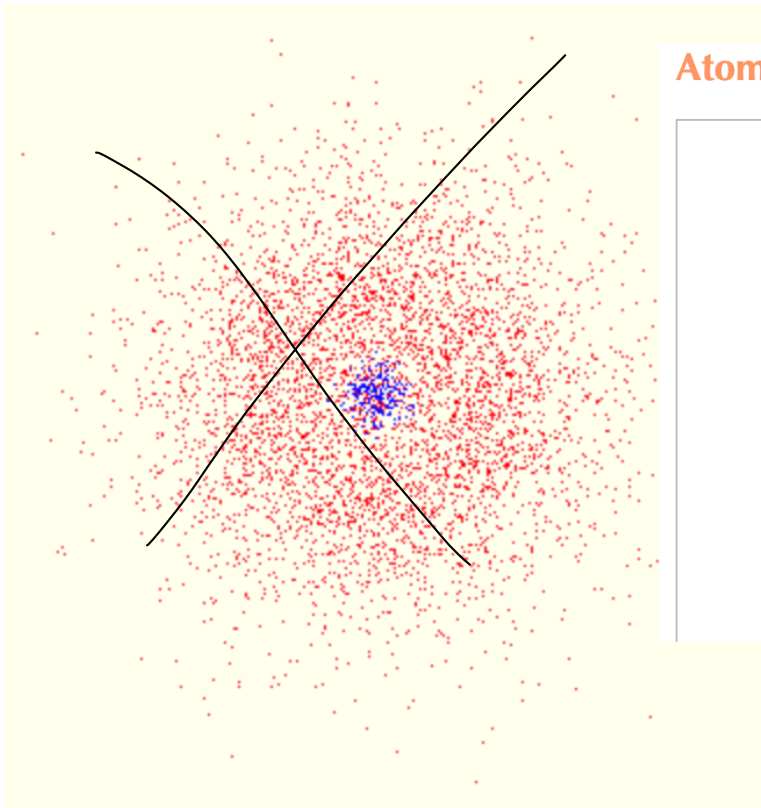


**The shape of the 2s orbital.** The blue zone is where the wave function has negative values while the red zone is where values are positive.

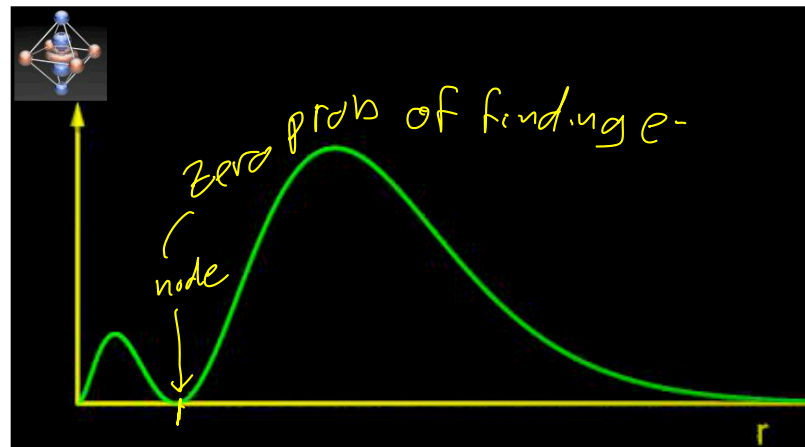
spherical  
b/c "s"

nodal surface  
or spherical  
node in betw  
spheres

prob of  
 $e^-$  at node



Atomic orbitals: 2s radial distribution function



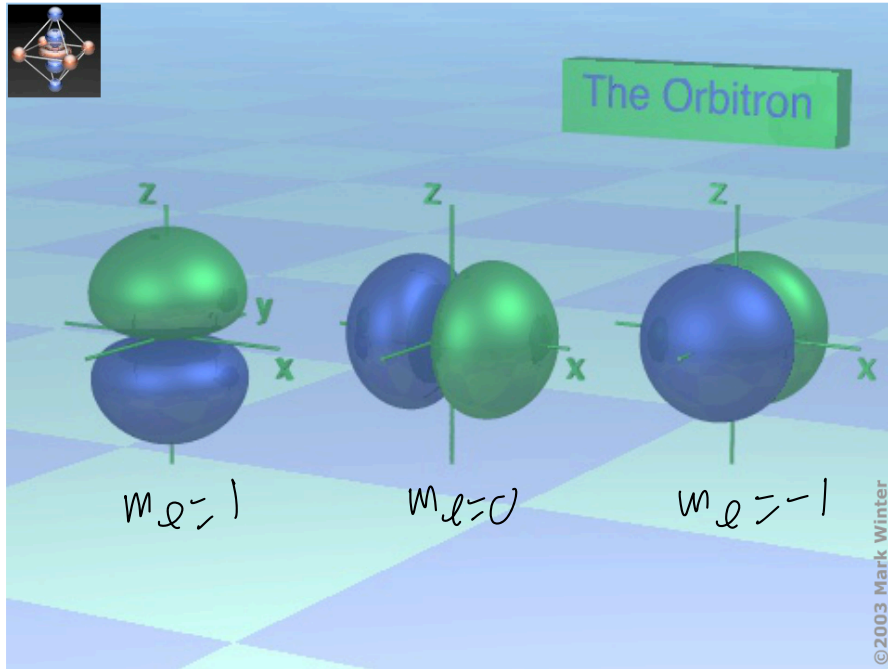
# 2p orbital

$l=1$

$n=2$

$l=1$

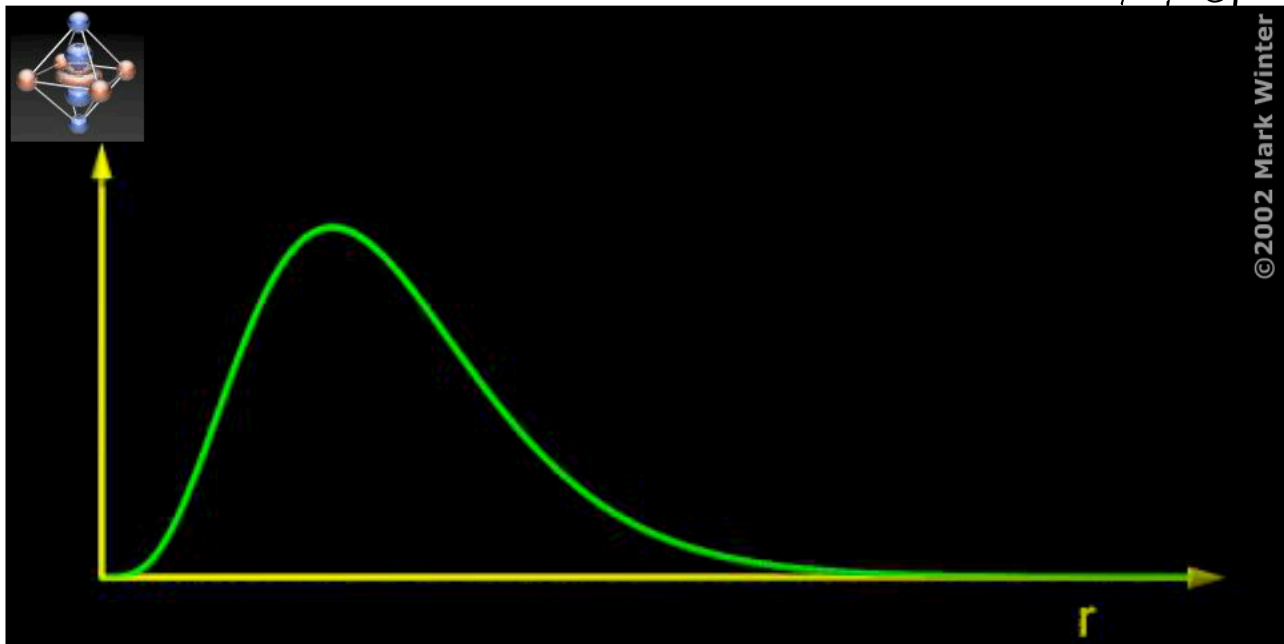
$m_l = -1, 0, 1$



no spherical node  
yes nodal plane  
between  
mushroom  
caps

**The shape of the three 2p orbitals.** From left to right:  $2p_z$ ,  $2p_x$ , and  $2p_y$ . For each, the blue zones are where the wave functions have negative values and the green zones denote positive values.

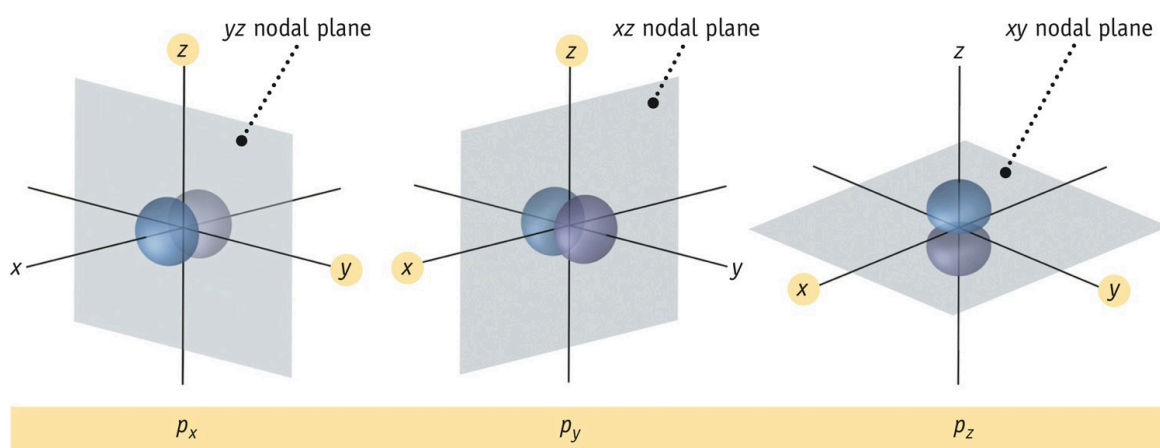
**Atomic orbitals: 2p radial distribution function** — for all 3 mashed together



**Schematic plot of the 2p radial distribution function  $r^2 R_{2p}^2$**  ( $R_{2p}$  = radial wave function).



# $p$ -Orbitals



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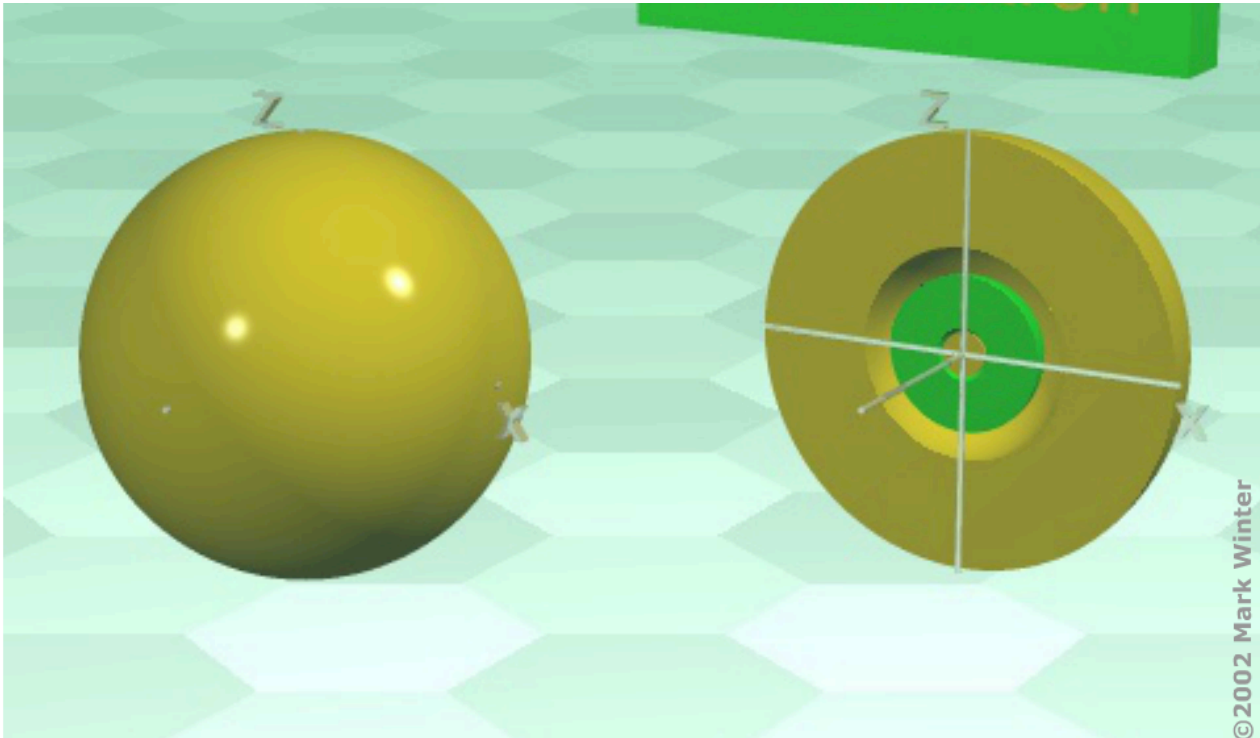
The three degenerate  $p$ -orbitals spread out on the  $x$ ,  $y$  &  $z$  axis,  $90^\circ$  apart in space.

# 3s orbital

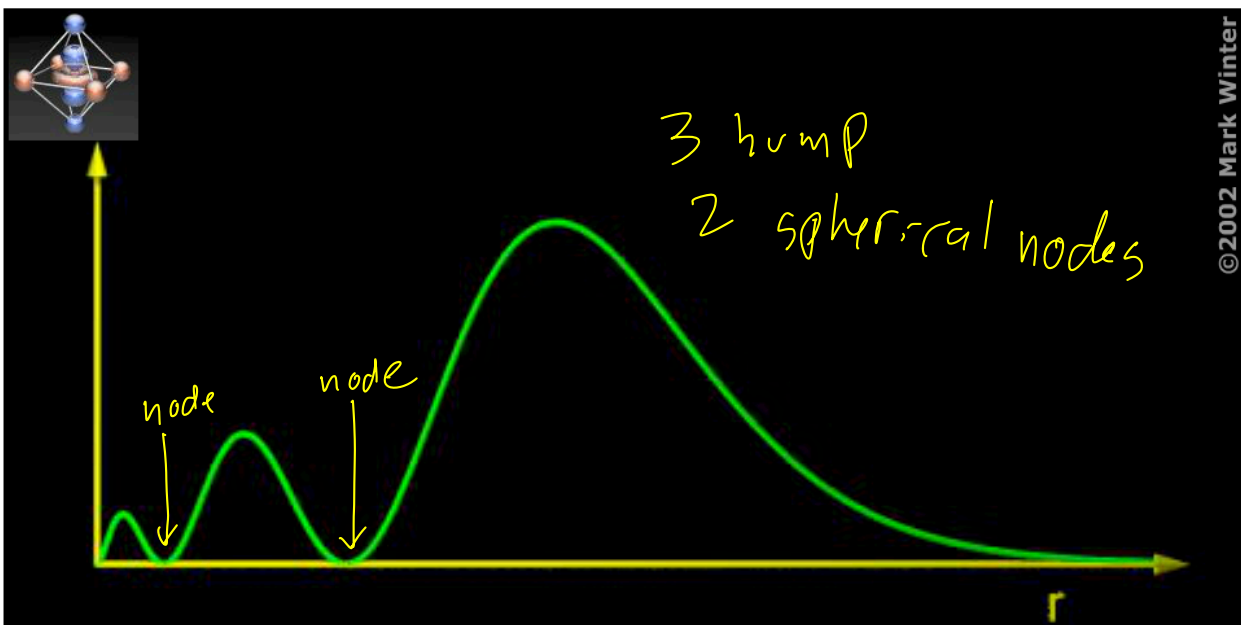
$$n=3$$

$$l=0$$

$$m_l=0$$



## Atomic orbitals: 3s radial distribution function



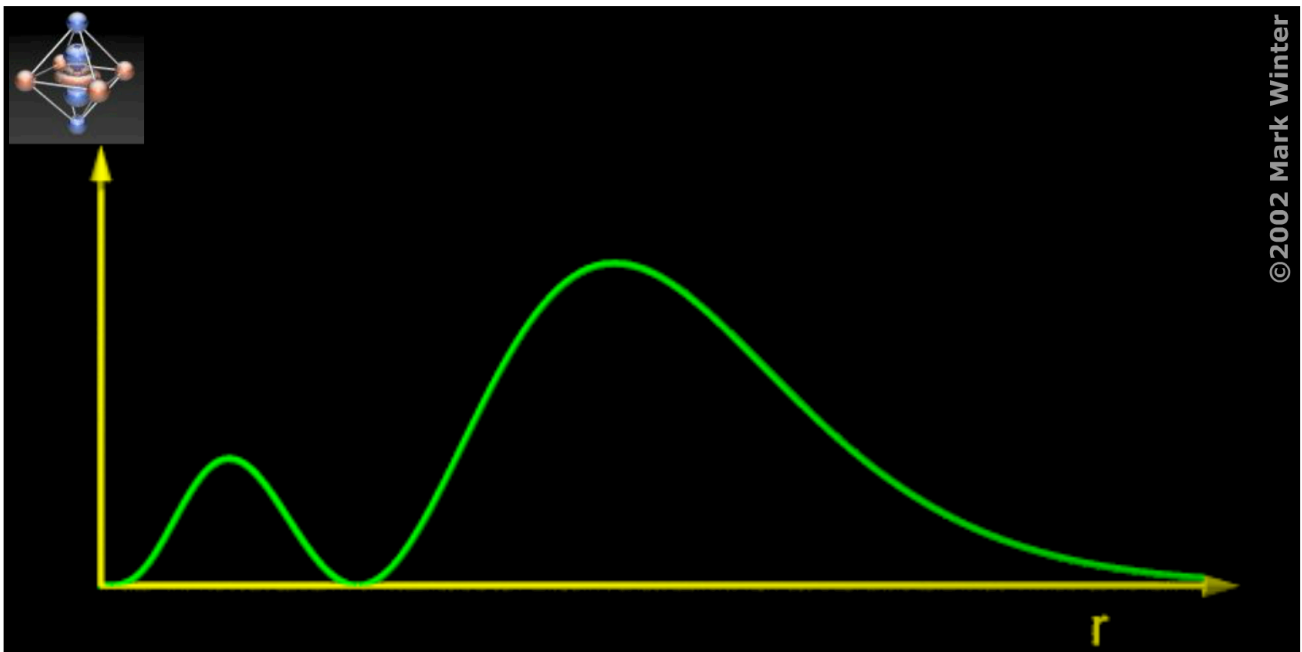
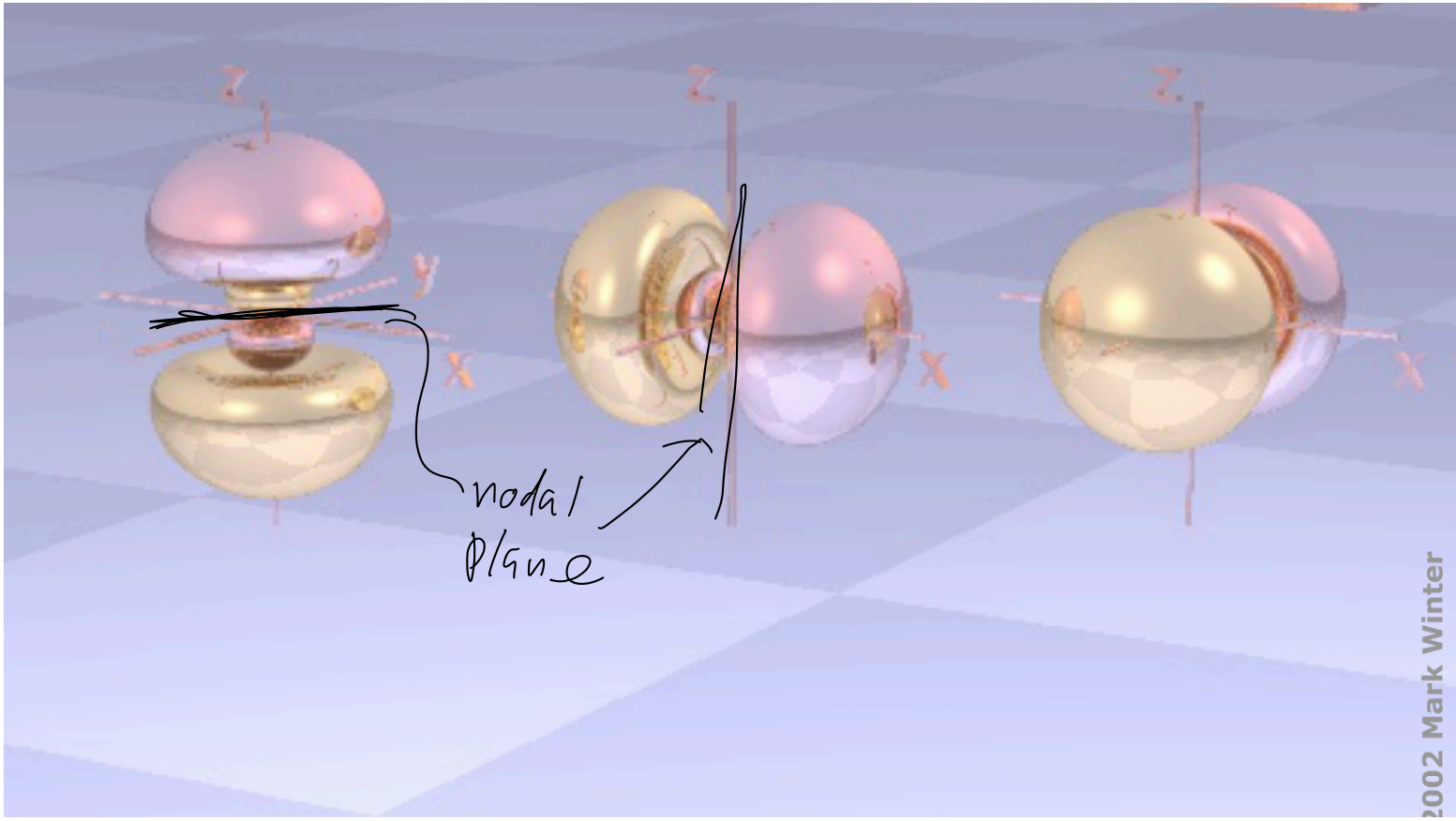
**Schematic plot of the 3s radial distribution function  $4\pi r^2 \psi_{3s}^2$ .** Blue represents regions within which the wave function is negative and red represents regions where the wave function is positive.

# 3p orbital $m$

$$n=3$$

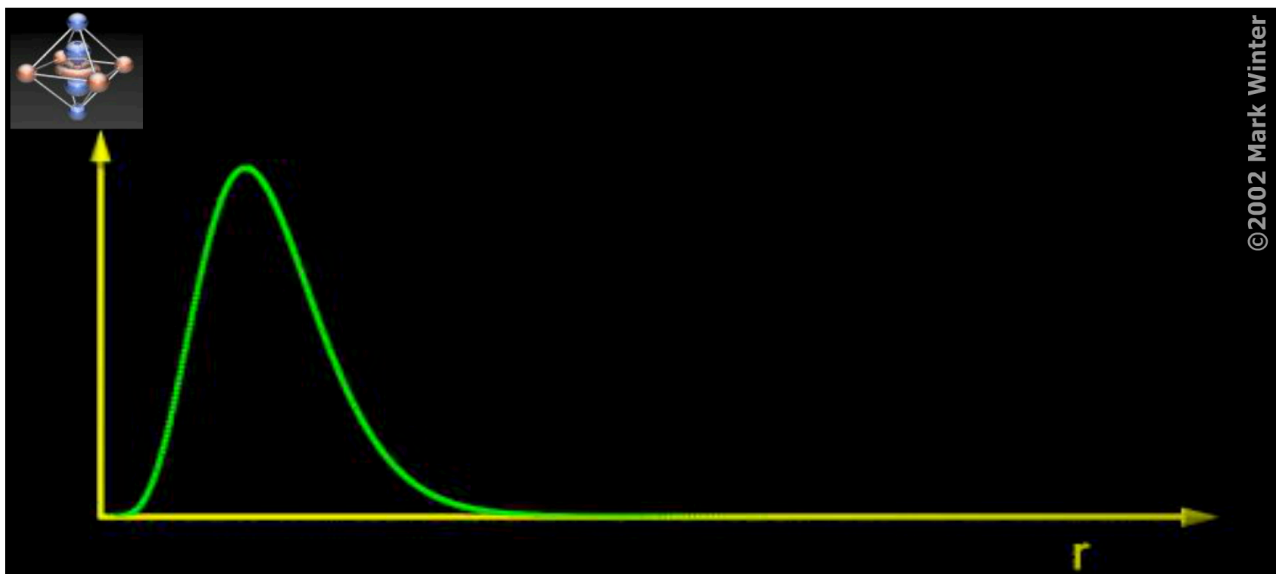
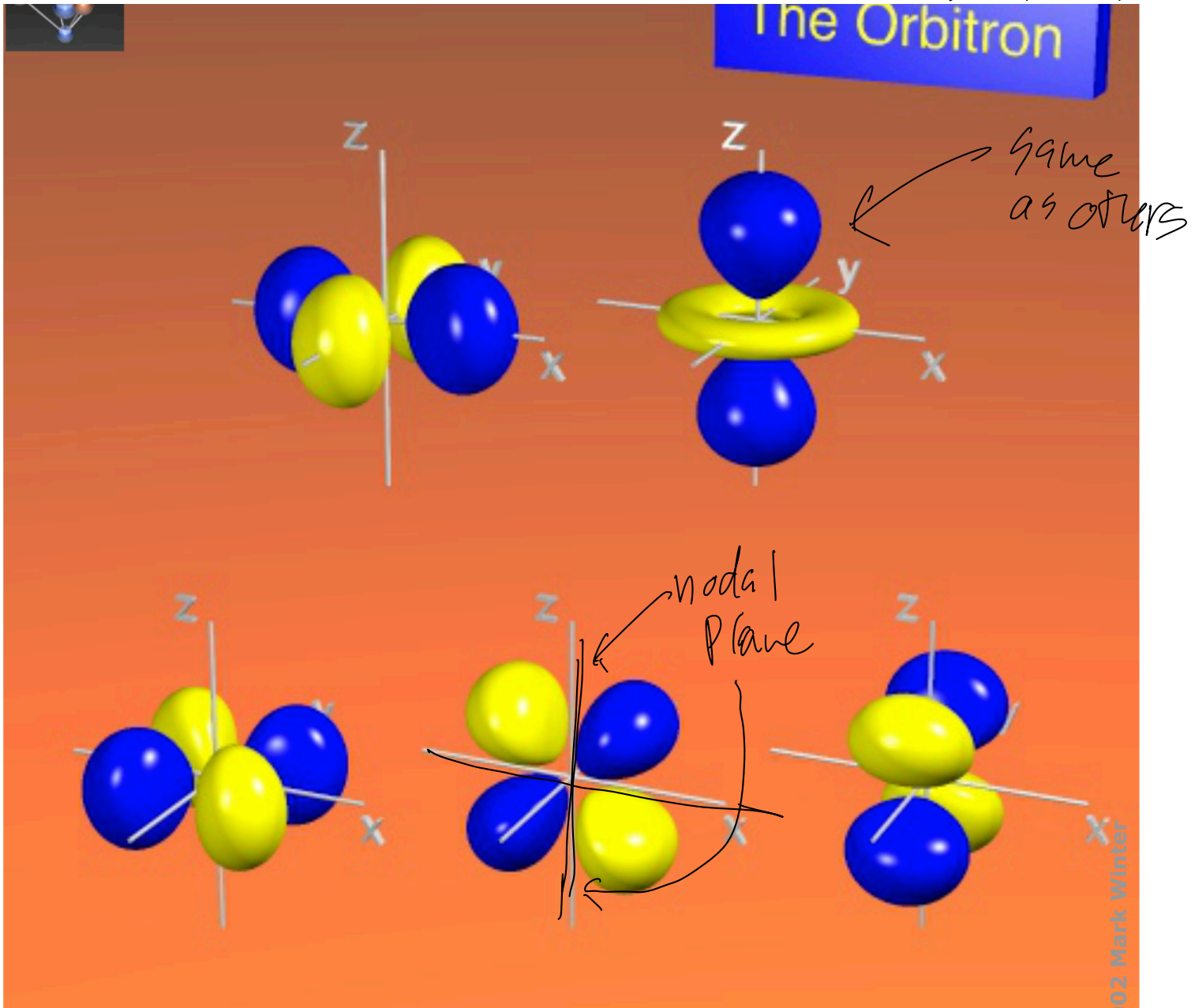
$$l=1$$

$$m_l = -1, 0, 1$$



**Schematic plot of the 3p radial distribution function  $r^2 R_{3p}^2$  ( $R_{3p}$  = radial wave function).**

# 3d orbital $n=3$ $l=2$ $m_l = -2, -1, 0, 1, 2$

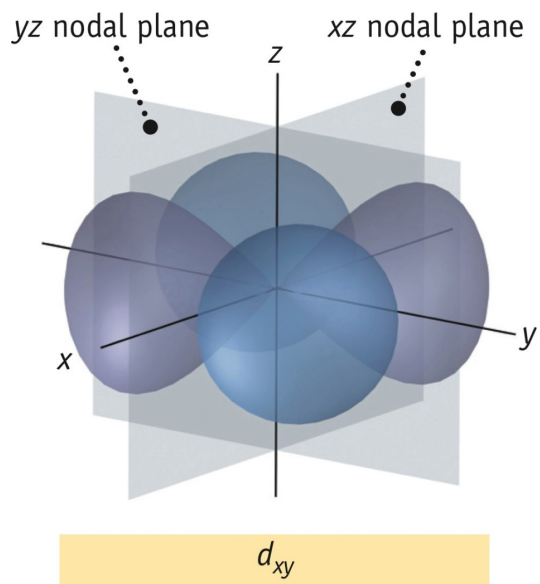


# $d$ -Orbitals

$s$ -orbitals have no nodal planes ( $l = 0$ )

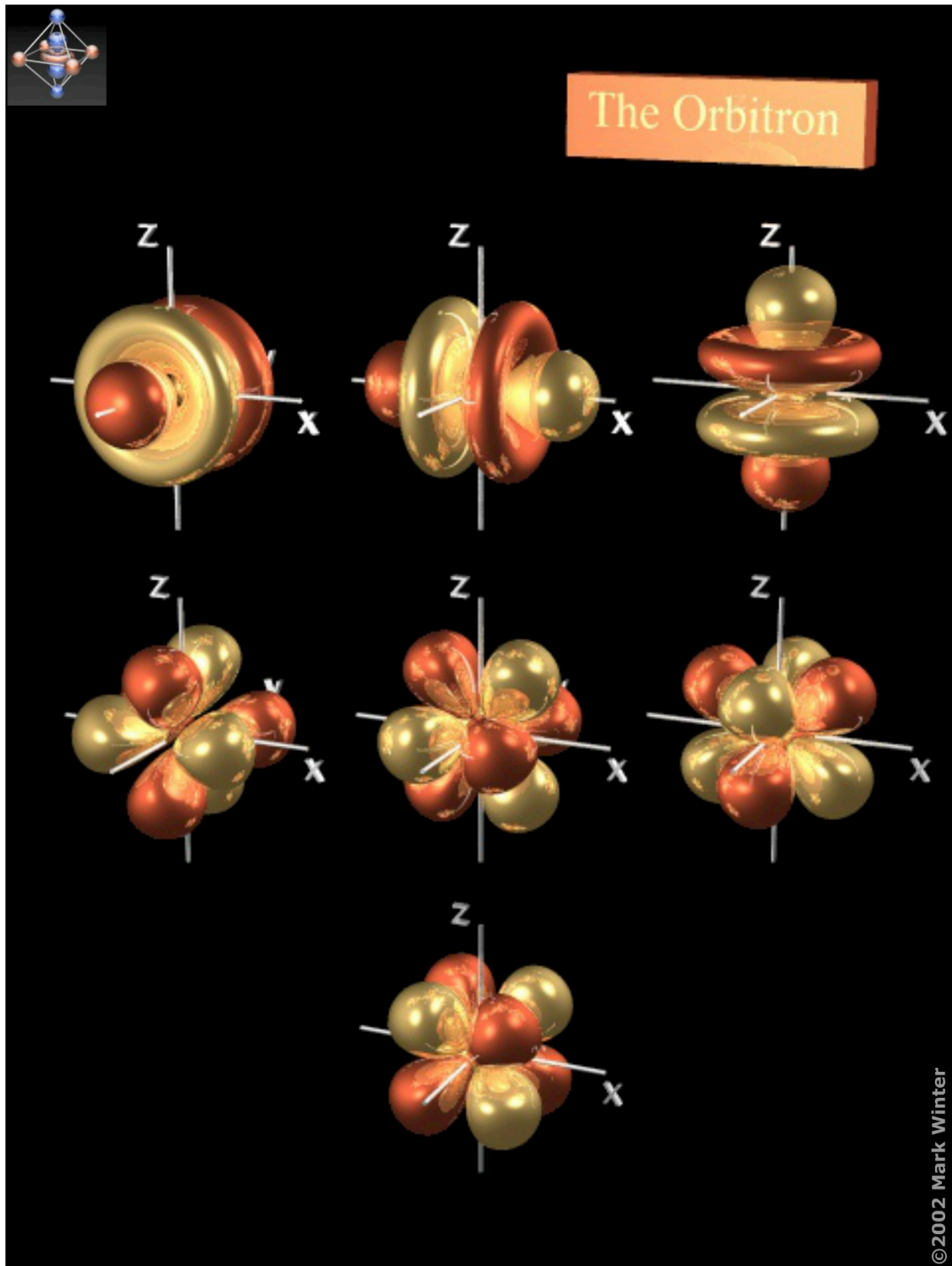
$p$ -orbitals have one nodal plane ( $l = 1$ )

$d$ -orbitals therefore have two nodal planes ( $l = 2$ )



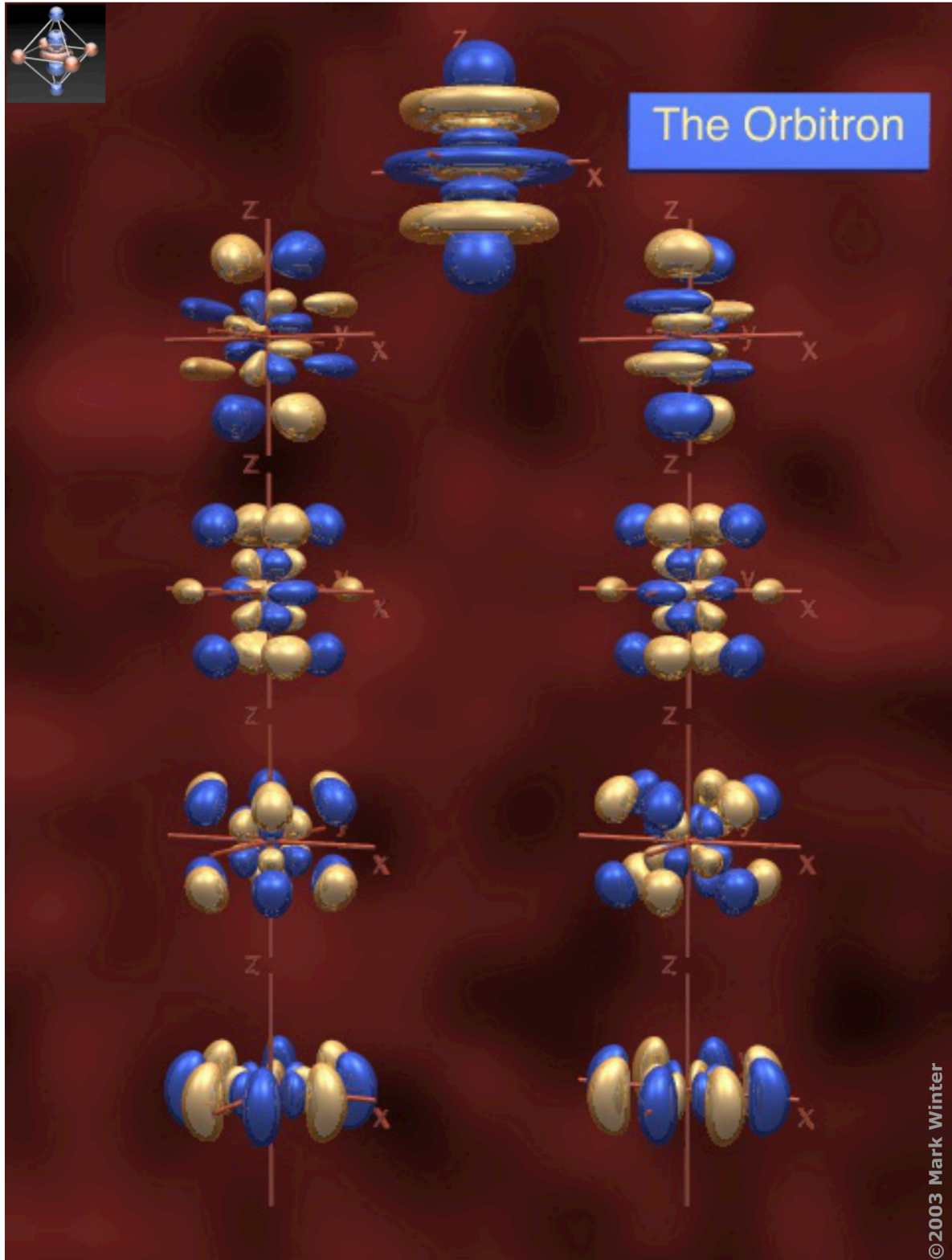


# Crazy orbital (4f)





# Bananas orbital (6g)





There is a 4<sup>th</sup> quantum number

$M_s$  electron spin QN

$$M_s = +\frac{1}{2} \text{ or } -\frac{1}{2}$$

Every electron <sup>in an atom</sup> must have its own unique set of 4 quantum numbers

$n$	$l$	$m_l$	$m_s$
1	0	0	$+\frac{1}{2}$
1	0	0	$-\frac{1}{2}$

not attracted to mag. field  
diamagnetic when all  $m_s$  of all  $e^-$  adds to zero

paramagnetic when all  $m_s$  of all  $e^-$  doesn't add to zero  
↳ will be attracted to mag. field

Avg 89%

Med 97%

100+ -23

90s -18

80s -6

<80s -13