

Mathematics Placement Test  
Practice Problems  
Section I

The following questions are a sample of the types of problems you might see on the Mathematics Placement Test. **Calculators are not permitted for the test.**

1. Express  $\frac{5}{2} \times \left( \frac{1}{11} - \frac{1}{2} \right)$  as a single fraction.  $\frac{5}{2} \left( \frac{2-11}{22} \right) = \frac{-5 \cdot 9}{44} = \boxed{-\frac{45}{44}}$

2. Is  $\frac{3}{5} < \frac{2}{3} < \frac{8}{14}$  true?  $\frac{9}{10} \stackrel{?}{<} \frac{10}{9} \checkmark$   $\frac{28}{24} \stackrel{?}{<} \frac{24}{28} \boxed{\text{No}}$

3. Factor the expression  $3x^2 + 5x - 2$ .  $\boxed{(3x - 1)(x + 2)}$

4. Simplify the expression  $\sqrt{\frac{18x^5}{z^2}}$ .  $\boxed{\frac{3x^2}{z} \sqrt{2x}}$

5. Expand  $4(s + 2)$ .  $\boxed{4s + 8}$

6. If  $x - 1 = 2$ , then what is  $x + 1$ ?  $x - 1 = 2 \Rightarrow x = 3 \Rightarrow \boxed{x + 1 = 4}$

7. If  $x = 3$ , then what is  $x^2 + 3$ ?  $3^2 + 3 = \boxed{12}$

8. Simplify the expression  $13a - 15b - a + 2b$ .  $(13a - a) - (15b - 2b) = \boxed{12a - 13b}$

9. If  $x = -4$  and  $y = -7$ , then what is  $x - y$ ?

$x - y = (-4) - (-7) = -4 + 7 = \boxed{3}$

10. Simplify  $\frac{(-2)(-6)}{-4}$ .  $\frac{12}{-4} = \boxed{-3}$

11. Simplify  $4 - (-2 + 5)$ .  $4 - (-2) - 5 = -1 + 2 = \boxed{1}$

12. Simplify  $(10) \left(\frac{1}{5}\right) (-2)(3)$ .  $= (2)(-6) = \boxed{-12}$

13. Solve for  $p$  in the following inequality:  $3p > p + 12$ .  $\Rightarrow 2p > 12 \Rightarrow \boxed{p > 6}$

14. Simplify the following expression  $(2x + 3) - (x - 2)$ .  $2x + 3 - x + 2 = \boxed{x + 5}$

15. If  $\frac{1}{3}$  of a number is 8, then what is  $\frac{1}{4}$  of the number?  $\frac{1}{3}x = 8 \Rightarrow x = 24$   
 $\Rightarrow \frac{1}{4}x = \boxed{6}$

16. Given that  $ax + b = 3$  and  $a \neq 0$ , solve for  $x$ .  $ax + b = 3 \Rightarrow \boxed{x = \frac{3-b}{a}}$

17. Simplify  $\frac{2x}{3y} \cdot \frac{9y}{4x^2}$ .  $= \boxed{\frac{3}{2x}}$

18. Determine the slope of the line that passes through the points  $(1, 1)$  and  $(-3, -2)$ .  $\text{slope} = \frac{-2-1}{-3-1} = \frac{-3}{-4} = \boxed{\frac{3}{4}}$

19. Factor the expression  $2x^2 - 7x + 6$ .  $\boxed{(2x - 3)(x - 2)}$

20. Factor the expression  $x^2 - 81$ .  $\boxed{(x - 9)(x + 9)}$

21. Simplify  $(-2x^2)(3x^2y)(-y)$ .  $= \boxed{6x^4y^2}$

22. Simplify  $(2x^5y^2)^2$ .  $\boxed{4x^{10}y^4}$

23. Simplify  $\frac{y}{x^3} \div \frac{y^3}{x}$ .  $\frac{y/x^3}{y^3/x} = \frac{\cancel{y}^1 \cdot \cancel{x}^1}{y^{\cancel{3}^2} \cdot x^{\cancel{3}^2}} = \boxed{\frac{1}{x^2 y^2}}$

24. If the sum of three numbers is 65 and one of the numbers is  $x$ , what is the sum of the other two?  $x + y = 65 \Rightarrow y = \boxed{65 - x}$

25. Factor the expression  $x^2 + x - 12$ .  $\boxed{(x - 3)(x + 4)}$

26. Factor the expression  $xy^4 + yx^4$ .  $\boxed{xy(y^3 + x^3)}$

27. Determine all the  $x$ -values that are solutions to  $x^2 + x - 1 = 0$ .  $x = \frac{-1 \pm \sqrt{1 - 4(-1)}}{2} = \boxed{\frac{-1 \pm \sqrt{5}}{2}}$

28. If  $5(2x + 3) - (x + 3) = 0$ , then what is  $x$ ?

$10x + 15 - x - 3 = 9x + 12 = 0 \Rightarrow 9x = -12 \Rightarrow x = \boxed{-\frac{12}{9} = -\frac{4}{3}}$

29. Expand  $(2m + 3)^2$ .

$(2m + 3)(2m + 3) = 4m^2 + 6m + 6m + 9 = \boxed{4m^2 + 12m + 9}$

30. The average of  $x$ ,  $y$  and  $z$  is 80. If two of the numbers are 74 and 78, then what is the other number?

$\frac{x + y + z}{3} = 80 \Rightarrow x + 74 + 78 = 240 \Rightarrow x = 240 - 74 - 78 = \boxed{88}$

31. Simplify the expression  $4^2 + 4^0$ .

$16 + 1 = \boxed{17}$

32. Simplify  $\sqrt{64x^{16}}$ .  $= \boxed{8x^8}$

33. Simplify  $\frac{6}{7} - \frac{1}{3}$ .  $\frac{18 - 7}{21} = \boxed{\frac{11}{21}}$

34. Simplify  $\frac{5}{7} \div \left(\frac{5}{9} + \frac{1}{7}\right)$ .  $\frac{5}{7} \div \frac{35 + 9}{63} = \frac{5}{7} \cdot \frac{63}{44} = \boxed{\frac{45}{44}}$

35. Simplify  $19.27 - 14.539$ .

$\boxed{4.731}$

36. Simplify  $(6.38)(0.542)$ .  $3.45796$

37. Simplify  $\frac{15M^2 + 5M}{5M}$ .  $3M + 1$

38. Simplify  $\frac{7}{3} \times \frac{1}{2}$ .  $\frac{7}{6}$

39. Evaluate  $x^2y - 2xy - y^2$  when  $x = -3$  and  $y = -4$ .  $-76$

40. Solve for  $x$  in the equation  $5x - 10 = 2 - 2x$ .  $x = 12/7$

41. Solve for  $x$  in the equation  $x^2 - 1 = 0$ .

$x = \pm 1$

42. Solve for  $x$  in the inequality  $1 - 5x < 3 + x$ .  $x > \frac{1}{3}$

43. Solve for  $x$  in the equation  $\frac{5}{10} = \frac{15}{x}$ .  $x = 30$

44. Perform the indicated operation and simplify the expression  $3x - (5x - 4)$ .

$3x - 5x + 4 = -2x + 4$

45. Perform the indicated operation and simplify the expression  $(x^2 - 2x + 2) - (4x^2 - 8x - 3)$ .

$x^2 - 4x^2 - 2x + 8x + 2 + 3 = -3x^2 + 6x + 5$

46. Expand the expression  $(4x - 5)(3x + 2)$ .

$12x^2 + 8x - 15x - 10 = 12x^2 - 7x - 10$

47. Solve for  $x$  in the equation  $x^2 - 3x + 1 = 0$ .

$x = \frac{3 \pm \sqrt{9 - 4(1)}}{2} = \frac{3 \pm \sqrt{5}}{2}$

48. Solve for  $a$  and  $b$  in the linear system

$$\begin{cases} 3a + b = 3 \\ a - 2b = 1 \end{cases} \quad \begin{array}{l} 6a + 2b = 6 \\ \underline{a - 2b = 1} \\ 7a = 7 \Rightarrow \boxed{a = 1} \\ 1 - 2b = 1 \Rightarrow \boxed{b = 0} \end{array}$$

49. Shade the region of the  $xy$ -plane described by  $\{(x, y) \mid x + 2y \geq 1\}$ .

50. Determine the equation for the line with slope  $1/3$  that passes through the point  $(3, -2)$ .  $\rightarrow y - (-2) = \frac{1}{3}(x - 3) \Rightarrow y = \frac{1}{3}x - 1 - 2$

