

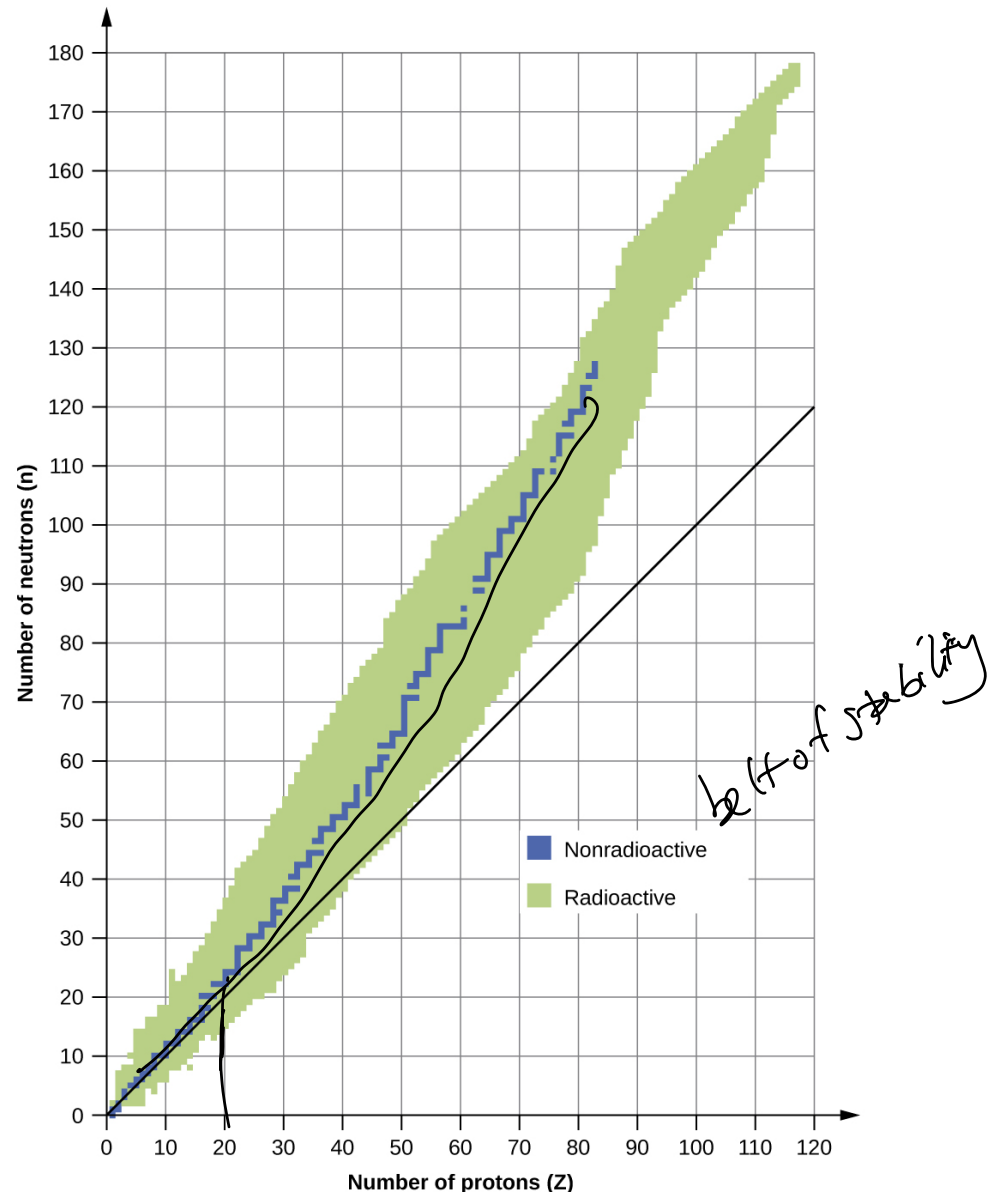
Isotopes

- Same number of protons but different number of neutrons
- Protons + neutrons are called nucleons







Radionuclides

- A nucleus is considered stable if it cannot transform without the addition of outside energy
- A radionuclide in contrast spontaneously decays into other nuclei until they reach a stable isotope

Belt of Stability



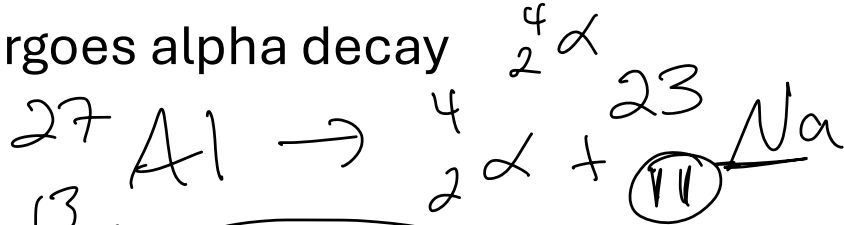
Types of Radioactive Decay

Name	Symbol(s)	Representation	Description
Alpha particle	${}^4_2\text{He}$ or ${}^4_2\alpha$		(High-energy) helium nuclei consisting of two protons and two neutrons
Beta particle	${}^0_{-1}\text{e}$ or ${}^0_{-1}\beta$		(High-energy) electrons
Positron	${}^0_{+1}\text{e}$ or ${}^0_{+1}\beta$		Particles with the same mass as an electron but with 1 unit of positive charge
Proton	${}^1_1\text{H}$ or ${}^1_1\text{p}$		Nuclei of hydrogen atoms
Neutron	${}^1_0\text{n}$		Particles with a mass approximately equal to that of a proton but with no charge
Gamma ray	γ		Very high-energy electromagnetic radiation

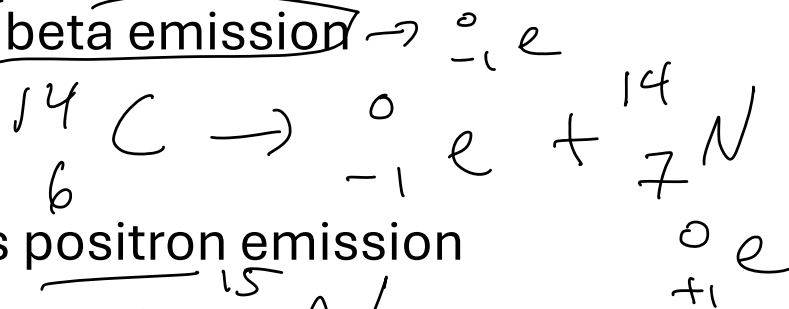
<https://openstax.org/books/chemistry-2e/pages/21-1-nuclear-structure-and-stability>

Writing Nuclear Equations

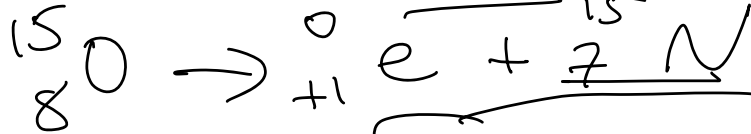
- Al-27 undergoes alpha decay



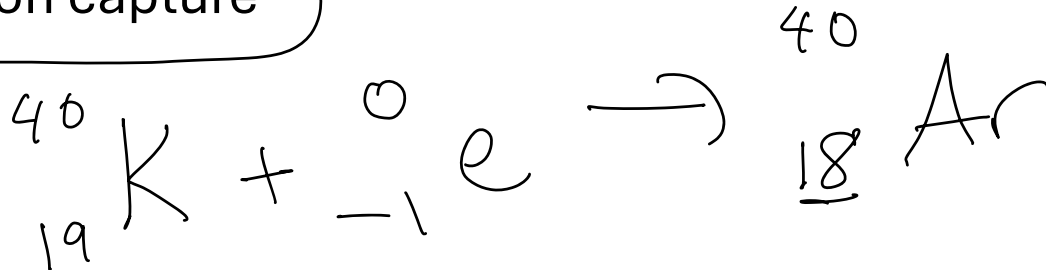
- C-14 decays by beta emission



- O-15 undergoes positron emission



- K-40 undergoes electron capture



• decay or emission
of a particle
products side

• capture particle
is on reactant
side.

Radioactive Decay

- Radioisotopes follow first order kinetics!

b/c

radioactive

- $\ln(N_t) = -kt + \ln(N_0)$ and $t_{1/2} = 0.693/k$

Example 1: Kinetics of Radioactive Decay

The half-life of cobalt-60 is 5.3 yr. How much of a 1.000-mg sample of cobalt-60 is left after 15.9 yr?

$$\ln 2 = \frac{0.693}{K}$$

$$\ln N_t = -kt \ln N_0$$

or

$$\frac{1}{2} \text{ lives } \frac{15.9 \text{ years}}{5.3 \text{ years}} =$$

3 1/2 lives

$$\frac{1}{2^3} = \frac{1}{8} \cdot (1.000 \text{ mg})$$

0.125 mg

Example 2: Kinetics of Radioactive Decay

A wooden object from an archeological site is subjected to radiocarbon dating. The activity of the sample that is due to ^{14}C is measured to be 11.6 disintegrations per second. The activity of a carbon sample of equal mass from fresh wood is 15.2 disintegrations per second. The half-life of ^{14}C is 5715 yr. What is the age of the archeological sample?

$$N_t = 11.6 \text{ dis/sec}$$

$$N_0 = 15.2 \frac{\text{dis}}{\text{sec}}$$

$$t_{y2} = \frac{0.693}{k}$$

$$k = \frac{0.693}{5.715 \text{ yr}}$$

$$k = 1.21 \times 10^{-4} \text{ yr}^{-1}$$

$$\ln N_t = -kt + \ln N_0$$

$$\ln N_t - \ln N_0 = -kt$$

$$\ln\left(\frac{N_t}{N_0}\right) = -kt$$

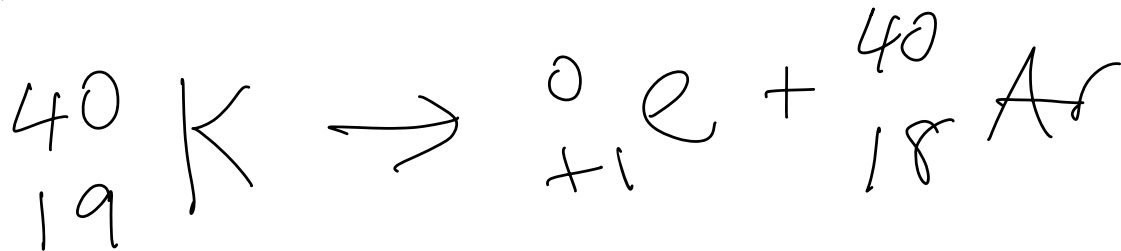
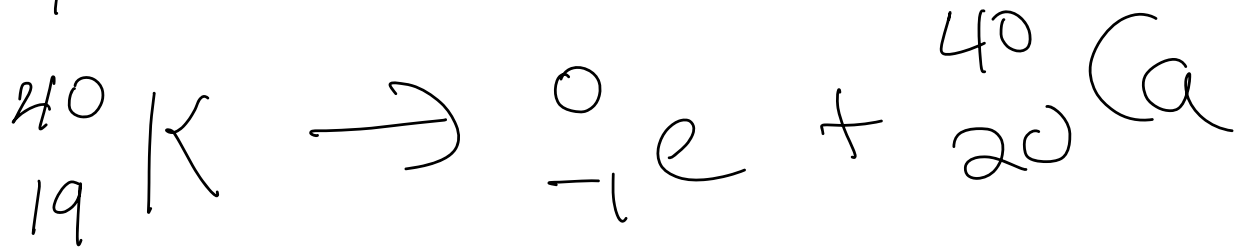
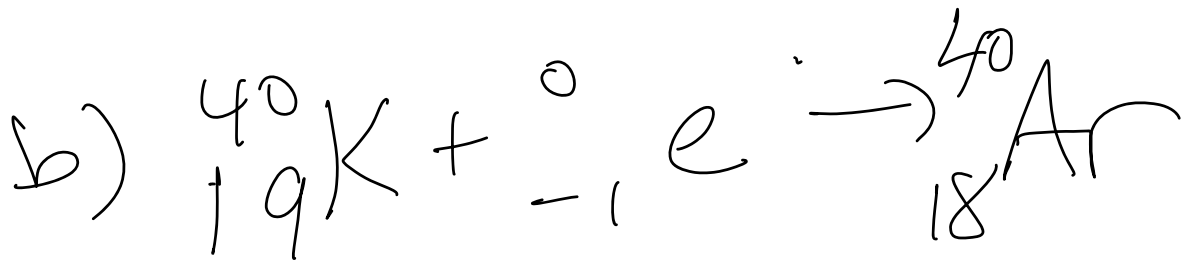
$$\ln\left(\frac{11.6}{15.2}\right) = -1.2 \times 10^{-4} \text{ yr}^{-1} (t)$$

$$t = 2,252 \text{ years}$$

Potassium ion is present in foods and is an essential nutrient in the human body. One of the naturally occurring isotopes of potassium, potassium-40, is radioactive. Potassium-40 has a natural abundance of 0.0117% and a half-life $t_{1/2} = 1.28 \times 10^9$ yr. It undergoes radioactive decay in three ways: 98.2% is by electron capture, 1.35% is by beta emission, and 0.49% is by positron emission. **(a)** Why should we expect ^{40}K to be radioactive? **(b)** Write the nuclear equations for the three modes by which ^{40}K decays. **(c)** How many $^{40}\text{K}^+$ ions are present in 1.00 g of KCl? **(d)** How long does it take for 1.00% of the ^{40}K in a sample to undergo radioactive decay?

a) ^{40}K

$19p + 21n > 1:1$ ratio
n: p 50
undergo to
radioactive
rxn.



c) ? K^+ ions present in
1.00g KCl

$$1.00 \text{ g KCl} \times \frac{1 \text{ mol KCl}}{74 \text{ g KCl}} \times \frac{1 \text{ mol } K^+}{1 \text{ mol KCl}} \times \frac{6.02 \times 10^{23} \text{ ions}}{1 \text{ mol } K^+}$$

$$8.1 \times 10^{21} K^+ \text{ ions}$$

$10^6 K^+$ is 0.0117% - $(8.1 \times 10^{21})(0.00017)$
 $9.5 \times 10^{17} K^+ \sim 40$

d) How long does it take for 1.00h of $k-90$ to decay?

$$\ln\left(\frac{N_t}{N_0}\right) = -kt$$

first find k

$$t_{1/2} = \frac{0.693}{k}$$

$$k = \frac{0.693}{1.28 \times 10^9 \text{ yr}}$$
$$k = 5.4 \times 10^{-10} \text{ yr}^{-1}$$

$$\frac{\ln(0.99)}{-5.4 \times 10^{-10} \text{ yr}^{-1}} = \frac{-5.4 \times 10^{-10} \text{ yr}^{-1} (t)}{-5.4 \times 10^{-10} \text{ yr}^{-1}}$$

$$t = 1.8 \times 10^7 \text{ years}$$

EPA Map of Radon Zones

